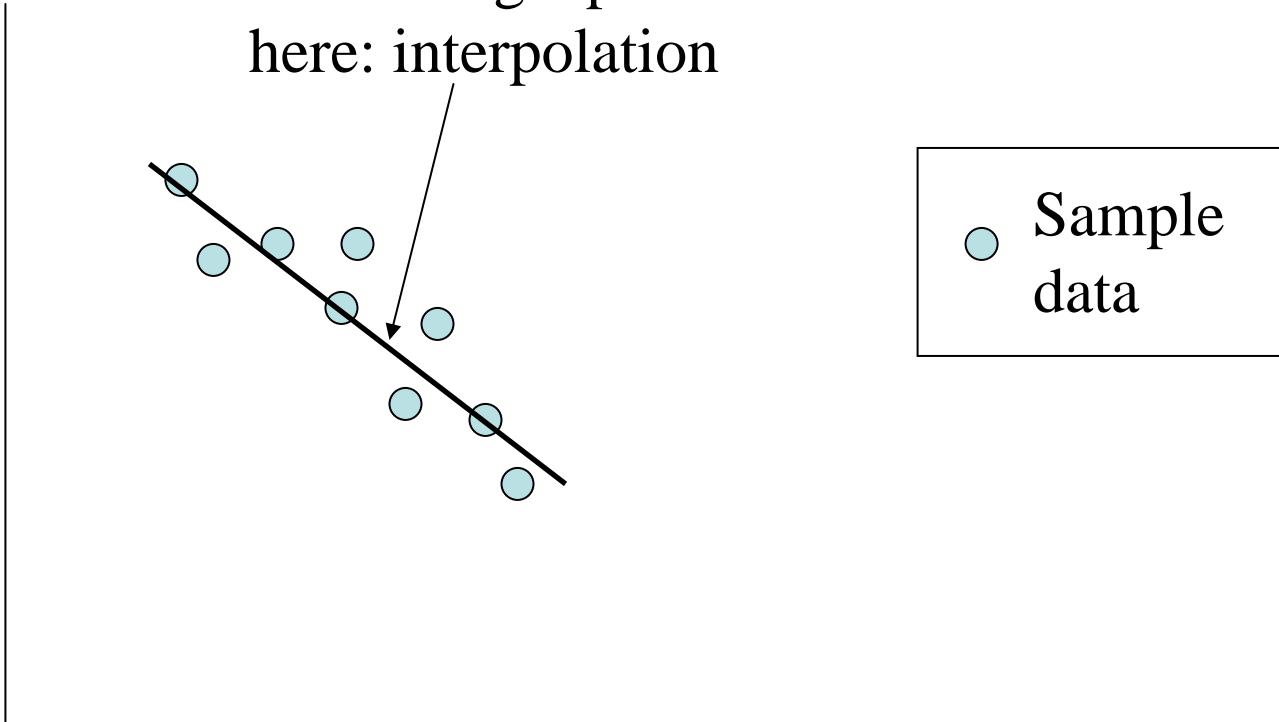


Spatial Interpolation

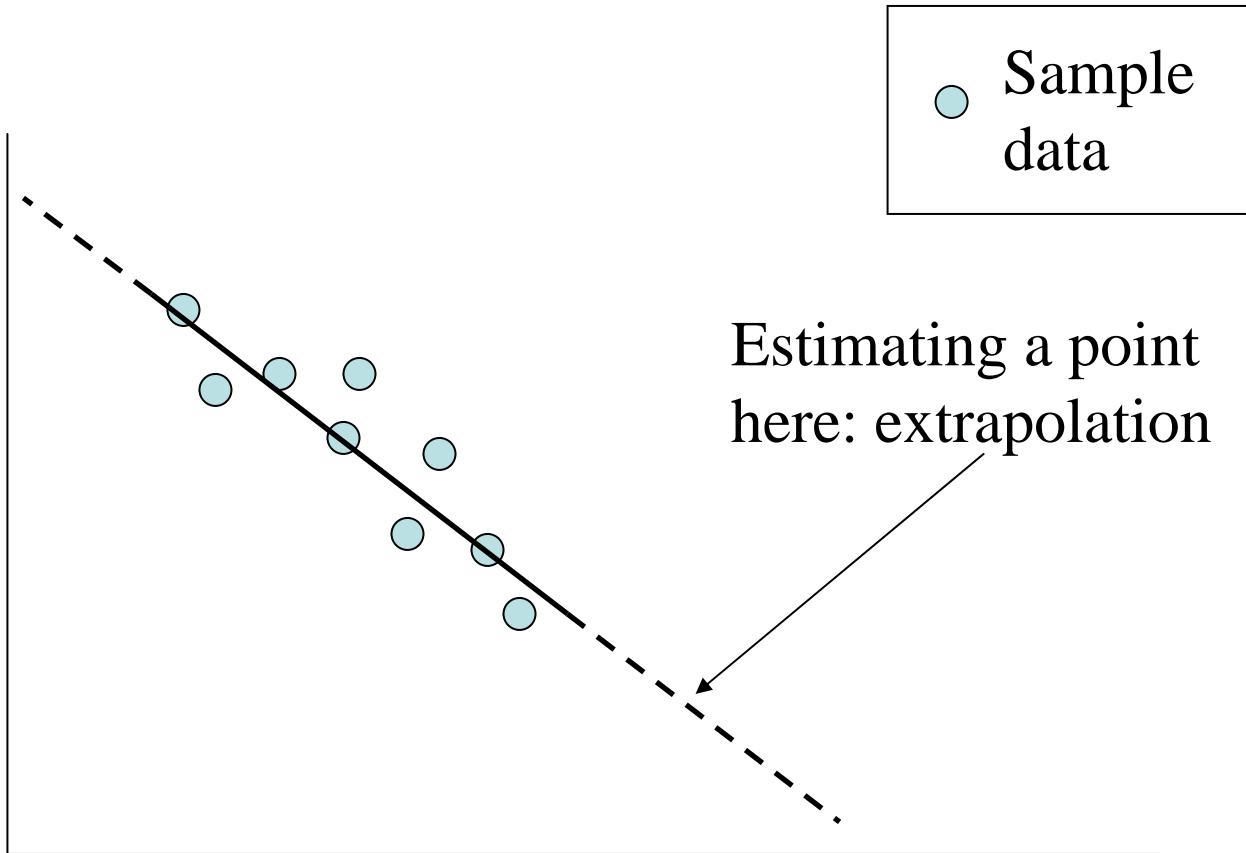
Spatial Interpolation is a process of using points with known values to estimate values at the other points.

Interpolation concept

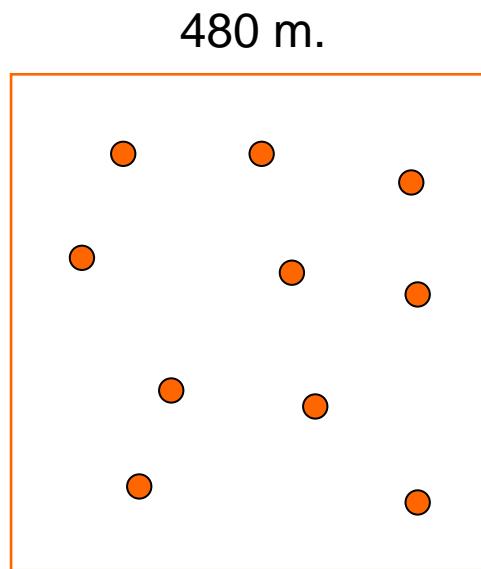
Estimating a point
here: interpolation



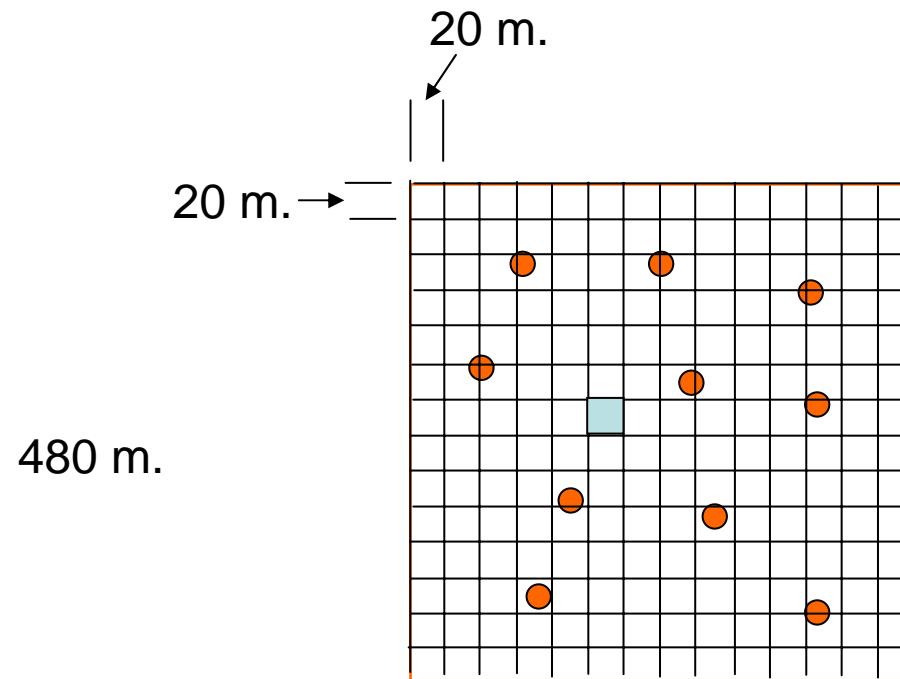
Extrapolation concept



Spatial Interpolation

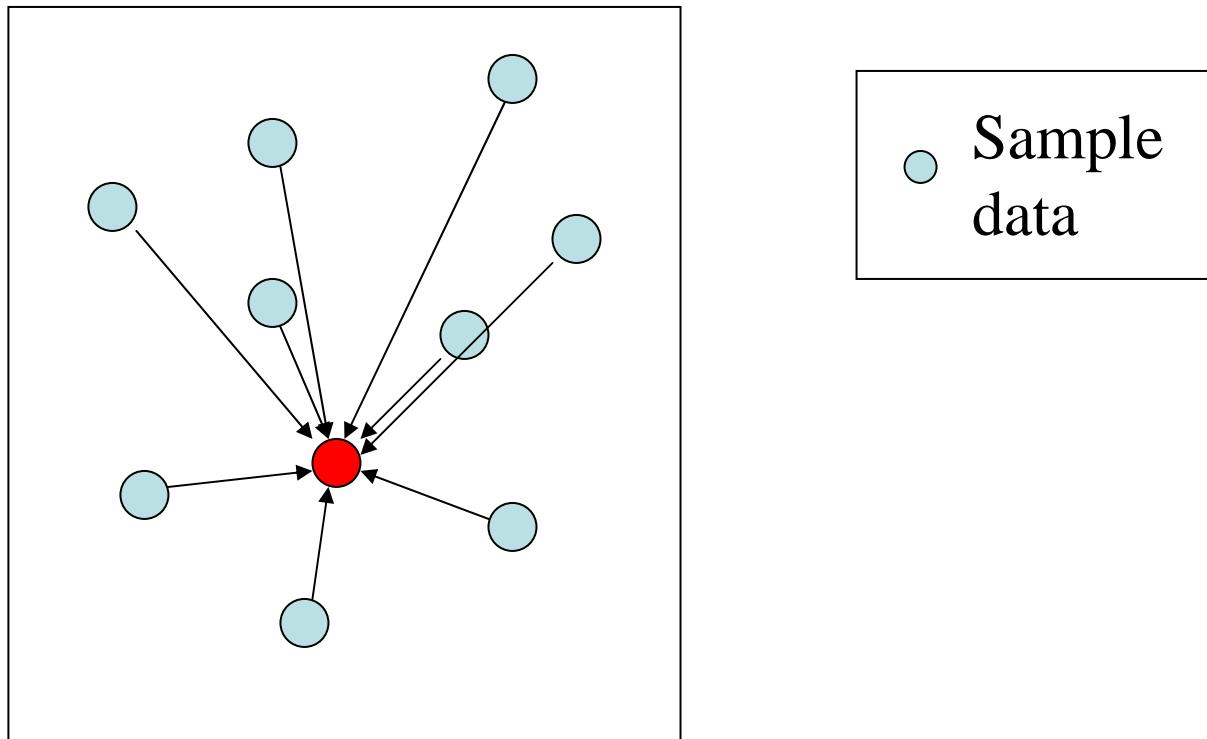


Sampling points



Global Interpolation

Uses all known sample points to estimate a value at an unsampled location

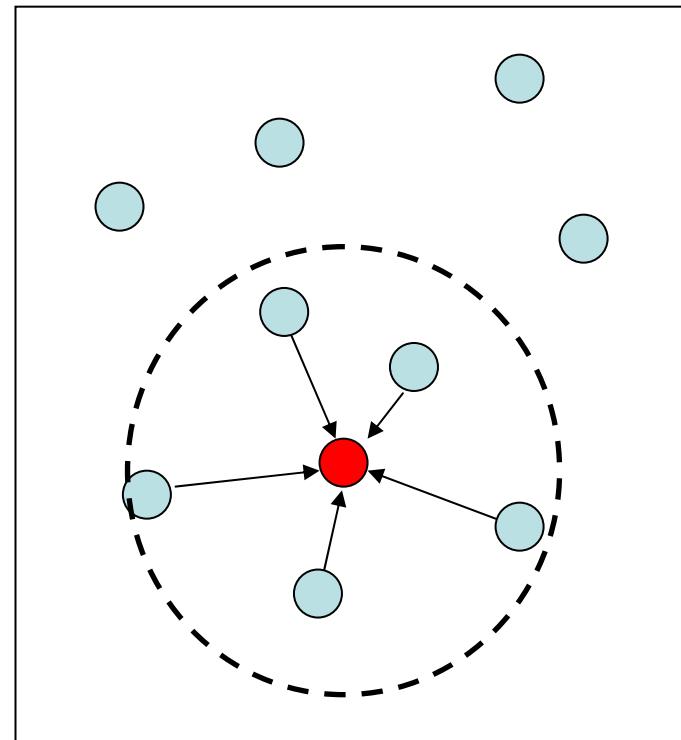
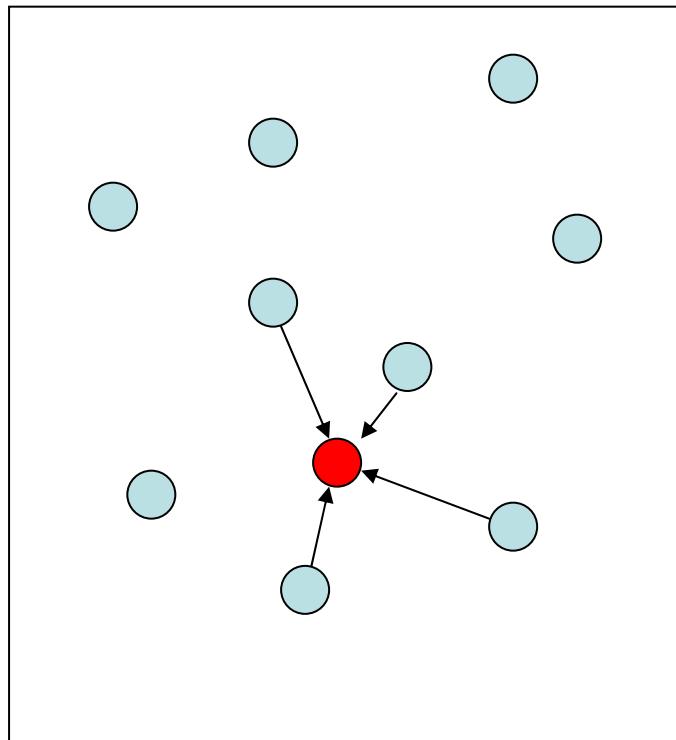


Local Interpolation

Uses a neighborhood of sample points to estimate a value at an unsampled location

Local neighborhood,

closest **4** number of points, or within a given search radius



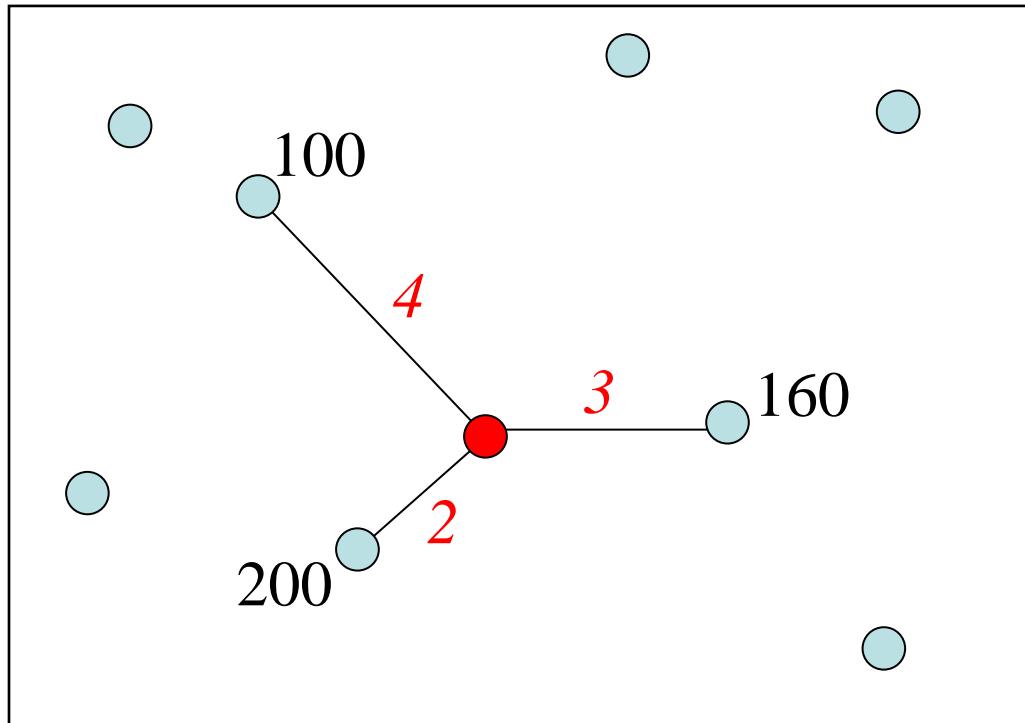
Spatial Interpolation Methods

There are a lot of methods

- Inverse distance weighting (IDW)
- Spline
- Trend surface
- Kriging
- etc.

Inverse Distance Weighted (IDW): Example

$$\hat{z}_j = \sum_{i=1}^m w_{ij} z_i \quad , \quad \text{where} \quad w_{ij} = \frac{1/d_{ij}^k}{\sum_{i=1}^m 1/d_{ij}^k}$$



$$z_i = 100, 160, 200$$

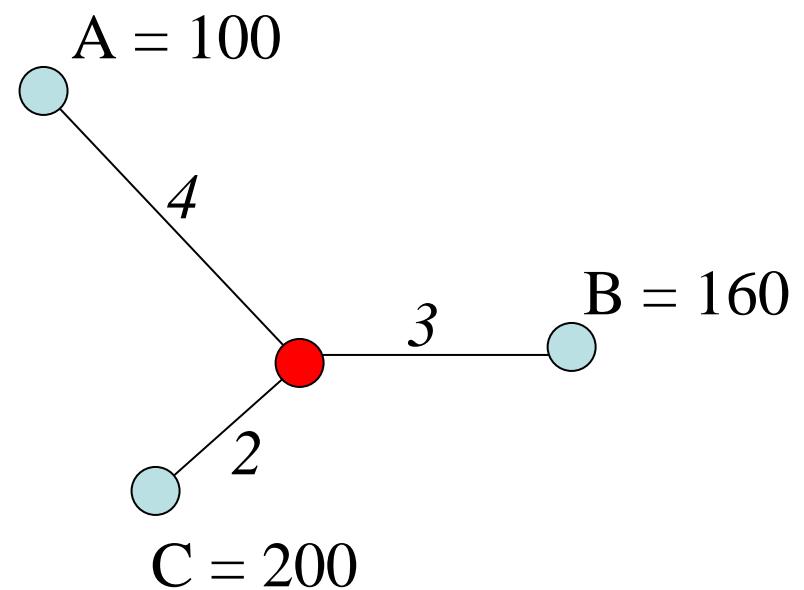
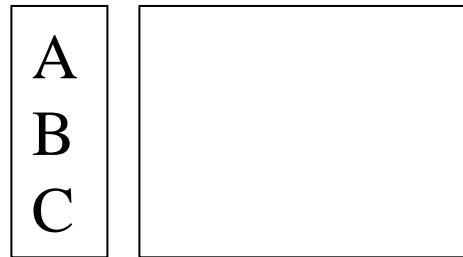
$$d_{ij} = 4, 3, 2$$

$$m = 3$$

$$k = 1$$

Inverse Distance Weighted (IDW): Example

$$1/d_{ij}^k$$



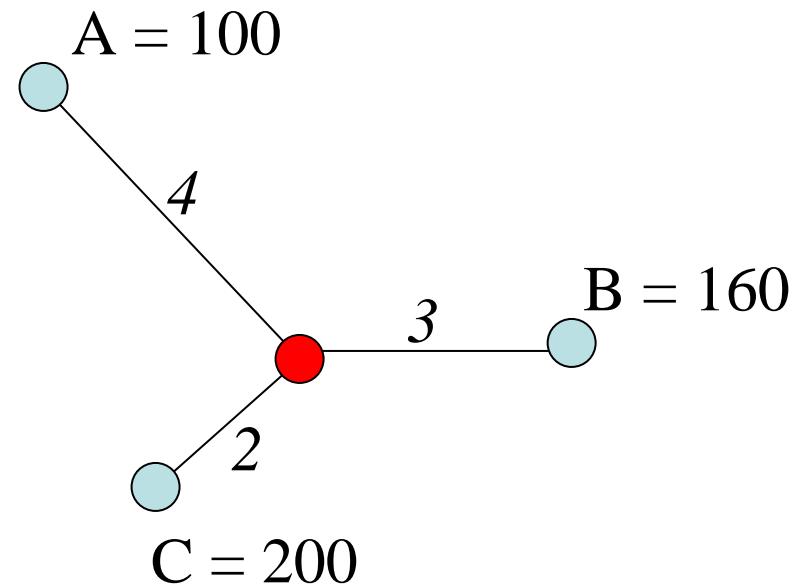
Inverse Distance Weighted (IDW): Example

$$1/d_{ij}^k$$

A
B
C

$1 / 4 = .25$
$1 / 3 = .33$
$1 / 2 = .50$

The weight = inverse of the distance



Inverse Distance Weighted (IDW): Example

$$1/d_{ij}^k$$

A
B
C

$$1/4 = .25$$

$$1/3 = .33$$

$$1/2 = .50$$

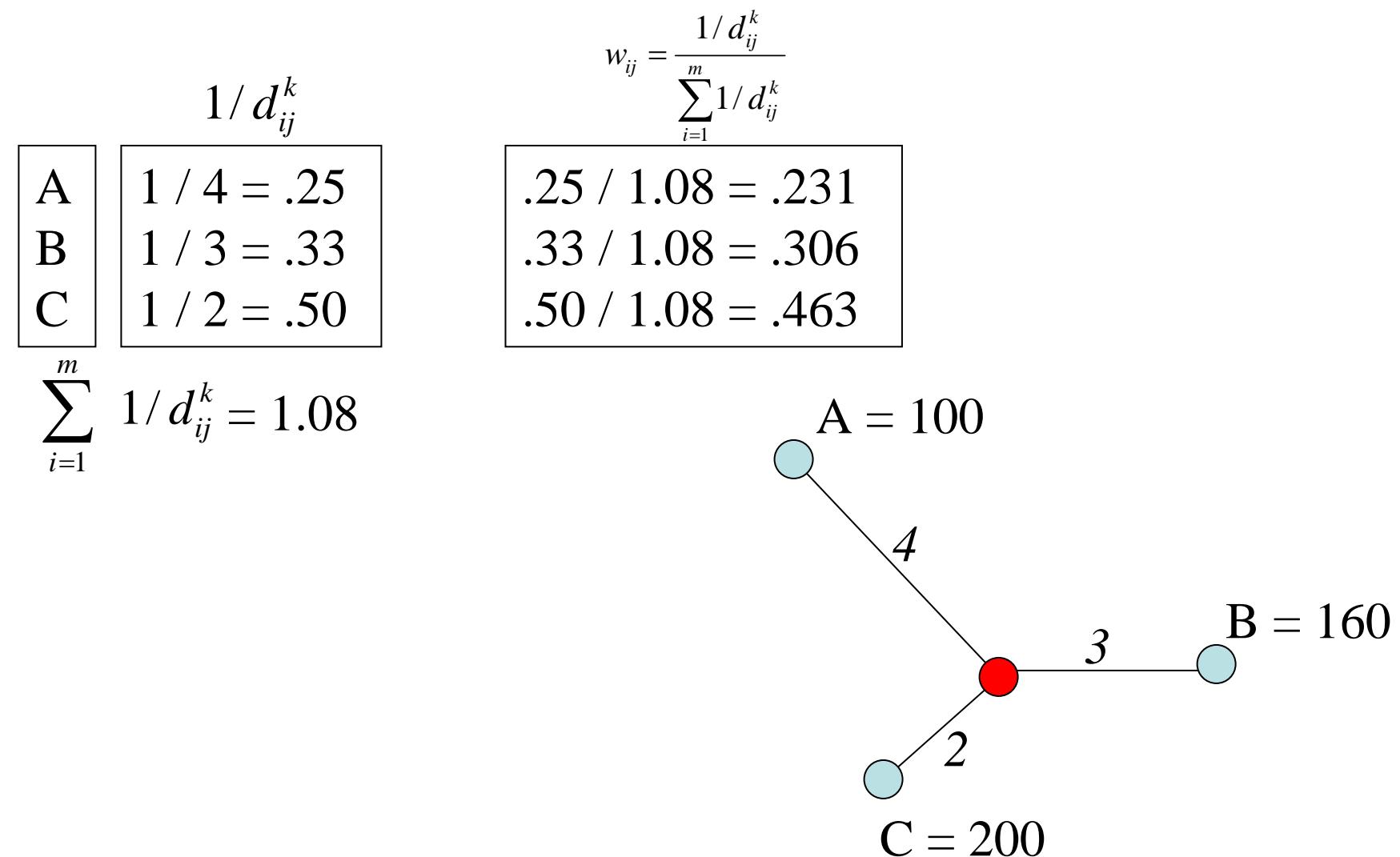
$$w_{ij} = \frac{1/d_{ij}^k}{\sum_{i=1}^m 1/d_{ij}^k}$$

$$.25 / 1.08 = .231$$

$$.33 / 1.08 = .306$$

$$.50 / 1.08 = .463$$

$$\sum_{i=1}^m 1/d_{ij}^k = 1.08$$



Inverse Distance Weighted (IDW): Example

$$1/d_{ij}^k$$

A
B
C

$$1/4 = .25$$

$$1/3 = .33$$

$$1/2 = .50$$

$$w_{ij} = \frac{1/d_{ij}^k}{\sum_{i=1}^m 1/d_{ij}^k}$$

$$w_{ij} z_i$$

$$.25 / 1.08 = .231$$

$$.33 / 1.08 = .306$$

$$.50 / 1.08 = .463$$

$$100 \times .231 = 23.1$$

$$160 \times .306 = 48.9$$

$$200 \times .463 = 92.6$$

$$\sum_{i=1}^m 1/d_{ij}^k = 1.08$$

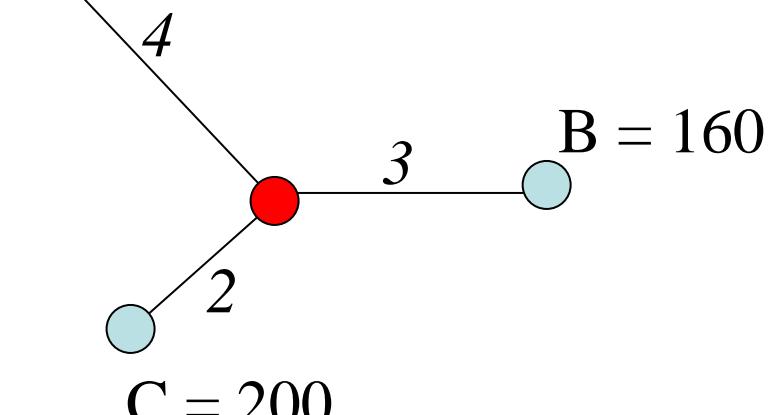
$$A = 100$$

$$4$$

$$B = 160$$

$$2$$

$$C = 200$$



Inverse Distance Weighted (IDW): Example

$$1/d_{ij}^k$$

A

$$1/4 = .25$$

B

$$1/3 = .33$$

C

$$1/2 = .50$$

$$w_{ij} = \frac{1/d_{ij}^k}{\sum_{i=1}^m 1/d_{ij}^k}$$

$$w_{ij} z_i$$

$$.25 / 1.08 = .231$$

$$.33 / 1.08 = .306$$

$$.50 / 1.08 = .463$$

$$100 \times .231 = 23.1$$

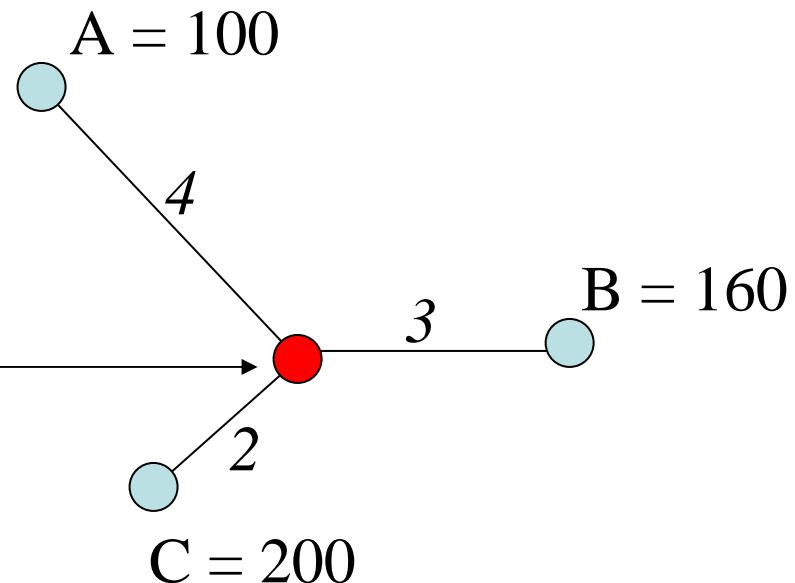
$$160 \times .306 = 48.9$$

$$200 \times .463 = 92.6$$

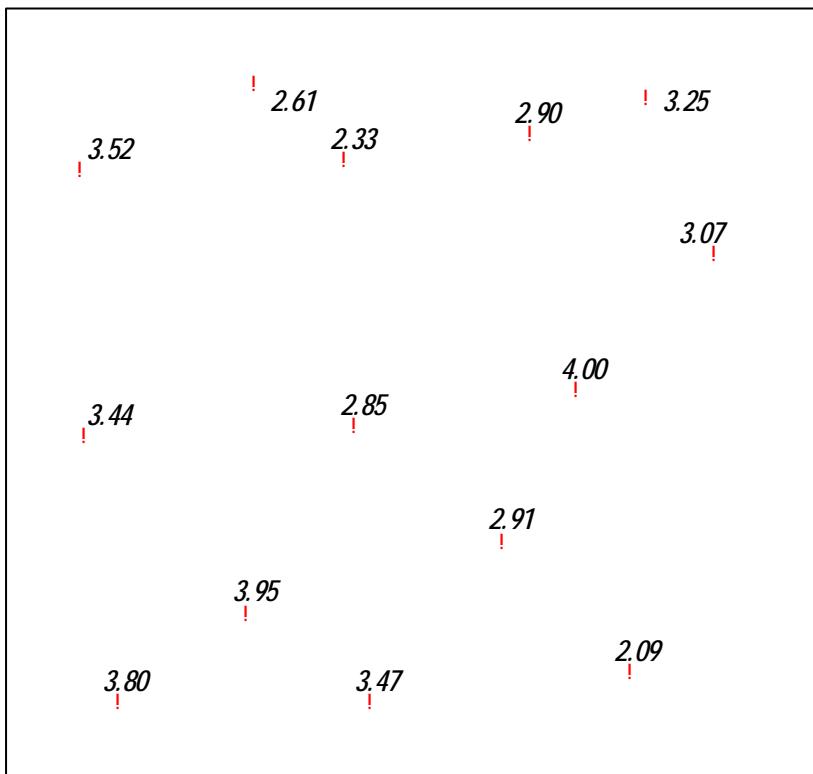
$$\sum_{i=1}^m 1/d_{ij}^k = 1.08$$

$$\hat{z}_j = \sum_{i=1}^m w_{ij} z_i$$

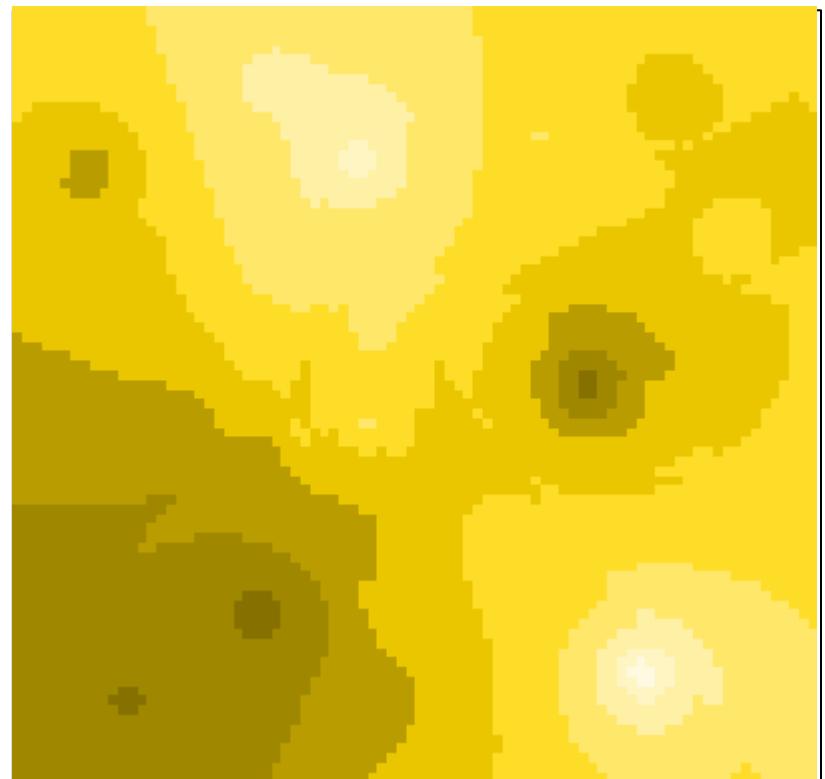
$$23.1 + 48.9 + 92.6 = \mathbf{164.6}$$



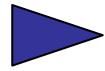
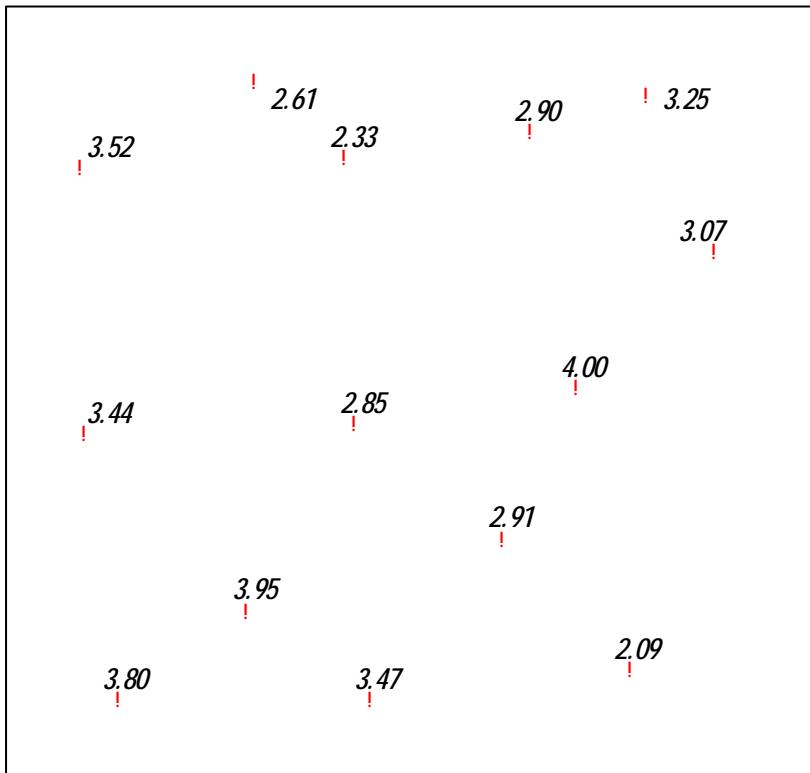
Sampling points



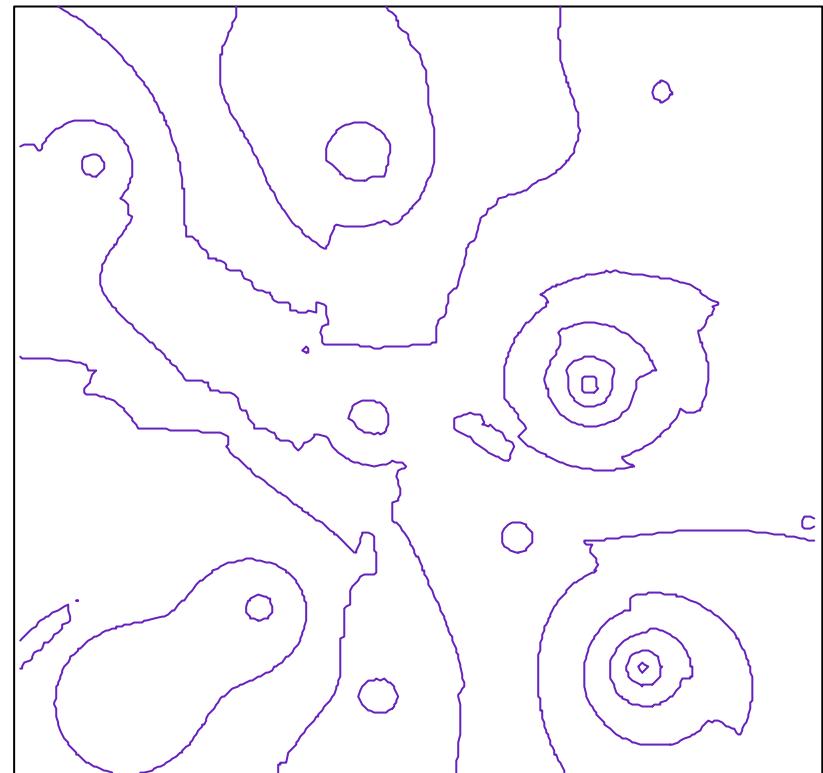
Surface



Sampling points



Contour



ArcView – Spatial Analyst Extension

